# EXCESS MOLAR ENTHALPIES OF THE TERNARY SYSTEM *p*-XYLENE+DECANE+DIETHYL CARBONATE

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Excess molar enthalpies of the ternary system  $\{x_1p$ -xylene+ $x_2$ decane+ $(1-x_1-x_2)$ diethyl carbonate $\}$  and the involved binary mixtures  $\{p$ -xylene+(1-x)decane $\}$ ,  $\{xp$ -xylene+(1-x)diethyl carbonate $\}$  and  $\{x$ decane+(1-x)diethyl carbonate $\}$  have been determined at the temperature of 298.15 K and atmospheric pressure, over the whole composition range, using a Calvet microcalorimeter. The experimental excess molar enthalpies  $H_m^E$  are positive for all the binary systems studied over the whole composition range. Excess molar enthalpy for the ternary system is positive as well, showing maximum values at  $x_1=0$ ,  $x_2=0.4920$ ,  $x_3=0.5080$ ,  $H_{m123}^E=1524$  J mol<sup>-1</sup>.

Keywords: decane, diethyl carbonate, excess molar enthalpies, ternary mixture, p-xylene

# Introduction

Continuing our previous studies on excess thermodynamic properties [1, 2], the present work reports experimental excess molar enthalpies of  $\{x_1p$ -xylene+  $x_2$ decane+ $(1-x_1-x_2)$  diethyl carbonate},  $\{xp$ -xylene +(1-x)decane},  $\{xp$ -xylene+(1-x)diethyl carbonate} and  $\{x$ decane+(1-x)diethyl carbonate} at the temperature of 298.15 K and atmospheric pressure. The measurement of excess molar enthalpies was carried out using a Calvet microcalorimeter. The results were fitted by means of different variable degree polynomials.

The thermophysical properties of binary mixtures of organic carbonates and *n*-alkanes have been studied by several workers. The excess molar enthalpies of {xdiethyl carbonate+(1-x)decane} and {xdiethyl carbonate+(1-x)p-xylene} at 298.15 K were measured by García *et al.* [3] and Lien *et al.* [4], respectively. Dominguez-Pérez *et al.* [13] have published data of excess molar enthalpy of {xxylene+ (1-x)hexane} at 298.15 K.

We are not aware of any previous measurement of of the ternary mixture to which this study is directed.

# **Experimental**

### Materials

The chemical substances employed were commercial products of the best quality grade (>099 mole fraction). Diethyl carbonate and p-xylene were supplied by Fluka, and decane was supplied by Aldrich. They

were subjected to no further purification other than drying with Union Carbide 0.4 nm molecular sieves to eliminate residual traces of water and degassed by ultrasound technique.

The handling and disposal of the chemicals used has been done according to the recommendation of the CRC Handbook of Chemistry and Physics [6].

### Methods

The mixtures were prepared by mass using a Mettler H51 balance (precision  $\pm 1 \cdot 10^{-5}$  g), ensuring a probable error in the mole fraction less than  $10^{-4}$ . All molar quantities are based on the IUPAC relative atomic mass table [7].

The experimental excess molar enthalpies were measured using a Calvet microcalorimeter equipped with a device allowing operation in the absence of vapour phase, and having a calorimeter-cell volume of approximately 10 cm<sup>3</sup>. A Philips PM2535 multimeter and a data acquisition system were linked to the micro-calorimeter. Calibration was performed electrically using a Setaram EJP30 stabilized current source. Further details about the experimental method of operation have been published [8, 9]. The apparatus and procedures were tested by determining excess enthalpies for the standard system hexane+cyclohexane at 298.15 K. The uncertainty in excess molar enthalpy measurements is estimated to be better than 1%.

Several experimental series of measurements were carried out for the ternary compositions resulting from adding diethyl carbonate to a binary mixture

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composed of  $\{x'_1p$ -xylene+ $x'_2$ decane $\}$ . The ternary composition point is then a pseudobinary mixture composed by addition of diethyl carbonate to the mentioned binary mixture. Thus, the ternary excess molar enthalpy at the pseudobinary composition  $x_1$ ,  $x_2$ ,  $(x_3=1-x_1-x_2)$  can be expressed as

$$H_{m,123}^{E} = H_{m,\phi}^{E} + (x_1 + x_2)H_{m,12}^{E}$$
(1)

where  $H_{m,\phi}^{E}$  is the measured excess molar enthalpy for the pseudobinary mixture and  $H_{m,12}^{E}$  is the excess molar enthalpy of the initial binary  $\{x_1'p\text{-xylene}+x_2'\text{dec-}ane\}$  mixture. Values of  $H_{m,12}^{E}$  at three mole fractions were interpolated by using a spline-fit method. Equation (1) does not involve any approximation.

## **Data correlation**

Experimental values of  $H_m^E$  for the {*xp*-xylene +(1-*x*)decane}, {*xp*-xylene+(1-*x*)diethyl carbonate} and {*x*decane+(1-*x*)diethyl carbonate} are listed in Table 1. The experimental data of  $H_m^E$  were fitted to the variable-degree polynomials, suggested by Redlich-Kister [10], of the form

$$H_{\rm m}^{\rm E}$$
 (J mol<sup>-1</sup>)=x(1-x) $\sum_{i=1}^{n} A_i (2x-1)^{i-1}$  (2)

The parameters  $A_i$  shown in Eq. (2) have been obtained by a fitting computer program which uses the least squares procedure and a Marquardt algorithm [11]. The number of parameters used was determined by applying the optimization F test [12]. These parameters and the standard deviations for  $H_m^E$  of the three binary mixtures involved in this ternary system are presented in Table 2.

Plots of the experimental values obtained together with the smoothing curves for  $H_m^E$  of the three involved binary systems are shown in Fig. 1. Literature data [3, 4] are also plotted.



Fig. 1 Excess molar enthalpies H<sup>E</sup><sub>m</sub>/J mol<sup>-1</sup> at 298.15 K of the three involved binary systems. Experimental values of:
 - {xp-xylene+(1-x)decane};

- $\blacksquare {xp-xylene+(1-x)diethyl carbonate} and$
- ▲ {xdecane+(1-x)diethyl carbonate}; – fitted by Eq. (2); ▼ … [3]; ◆ … [4]

The measured values of ternary excess properties  $H_{m,123}^{E}$ , listed in Table 3, were correlated using the following equation:

$$H_{m,123}^{E}$$
 (J mol<sup>-1</sup>)= $H_{m,bin}^{E} + x_{1}x_{2}(1 - x_{1} - x_{2})\Delta_{123}$  (4)

where

$$H_{\rm m,bin}^{\rm E} = H_{\rm m,12}^{\rm E} + H_{\rm m,13}^{\rm E} + H_{\rm m,23}^{\rm E}$$
(5)

is known as the binary contribution to the excess ternary properties and  $H_{m,ij}^{E}$  are given by Eq. (2).

The last term stands for the ternary contribution to the magnitude, which was correlated using the expression suggested by Nagata and Tamura [13]

$$\Delta_{123} = (B_0 + B_1 x_1 + B_2 x_2 + B_3 x_1^2 + B_4 x_2^2) \quad (6)$$

The  $B_i$  parameters were calculated by an unweighted least-squares method using a non-linear optimization algorithm due to Marquardt [11]. These

x	$H_{\rm m}^{\rm E}/{ m J}~{ m mol}^{-1}$	x	$H_{\rm m}^{\rm E}/{ m J}~{ m mol}^{-1}$	x	$H_{\rm m}^{\rm E}/{ m J}~{ m mol}^{-1}$		
<i>xp</i> -xylene+(1– <i>x</i> )decane							
0.0740 0.1406 0.2120 0.3076	71 132 183 244	0.3796 0.4761 0.6016 0.6898	282 312 325 304	0.7883 0.8958 0.9643	254 154 60		
		<i>xp</i> -xylene+(1– <i>x</i>	)diethyl carbonate				
0.1080 0.1776 0.2819	35 53 72	0.4027 0.4766 0.6115	82 83 78	0.7169 0.7909 0.8692	66 53 35		
		xdecane+ $(1-x)$	diethyl carbonate				
0.1597 0.2423 0.2965	891 1179 1316	0.3639 0.4815 0.5882	1438 1521 1482	0.6935 0.8413	1307 856		

**Table 1** Excess molar enthalpies,  $H_m^E$ , of the binary systems at the temperature 298.15 K

parameters and the corresponding standard deviation are included in Table 4.

Figure 2 shows the pseudobinary representation of the measured experimental values, of  $H_{m,123}^{E}$ , together with the correlated curves, where Eq. (6) was applied to fit the ternary contribution.

The lines of constant ternary excess molar enthalpy,  $H_{m,123}^{E}$  calculated using Eq. (4) are plotted in Fig. 3a. Figure 3b represents the ternary contribution  $x_1x_2(1-x_1-x_2)\Delta_{123}$ , to the excess molar enthalpy correlated with Eq. (6).

## **Results and discussion**

The experimental excess molar enthalpies  $H_m^E$  are positive for all the binary systems studied over the whole composition range. It suggests the predominance of breaking the previous interactions over the formation of new interactions during the mixing process.

García *et al.* [3] determined the  $H_m^E$  values for the system {xdecane+(1-x)diethyl carbonate} at 298.15 K obtaining  $H_m^E$  (x=0.5)=1536 J mol<sup>-1</sup> somewhat upper than our  $H_m^E$  (x=0.5)=1523 J mol<sup>-1</sup>. The dotted curve shown in Fig. 1 was calculated from the smoothing equation reported by those authors. Not differences are showing between our results and those obtained by Lien *et al.* [4].



Fig. 2 Pseudobinary representation of ternary excess molar enthalpies  $H_{m,123}^{E}/J \text{ mol}^{-1}$  for {(1-x)(x'\_{1}p-xylene +x'\_{2}decane)+xdiethyl carbonate} at 298.15 K: • - x'\_{1}=0.2558, x'\_{2}=0.7442; ▲ - x'\_{1}=0.5038, x'\_{2}=0.4920, • - x'\_{1}=0.7531, x'\_{2}=0.2469, -- correlated using Eq. (4)

**Table 2** Fitting parameters  $A_i$  for Eq. (2) and standard deviations, s

$A_1$	$A_2$	$A_3$	$A_4$	$A_5$	S		
<i>xp</i> -xylene+(1- <i>x</i> )decane							
1273	370	120			1		
xp-xylene+(1- $x$ )diethyl carbonate							
332	-36	51	0	-94	0.3		
xdecane+ $(1-x)$ diethyl carbonate							
6096	-165	912			4		

**Table 3** Experimental excess molar enthalpies,  $H_{m,123}^{E}$ , at the temperature 298.15 K for the ternary mixture:  $x_1p$ -xylene+ $x_2$ dec-ane+ $(1-x_1-x_2)$ diethyl carbonate<sup>a</sup>

$x_1$	<i>x</i> <sub>2</sub>	$H_{\mathrm{m,\phi}}^{\mathrm{E}}/\mathrm{J} \mathrm{mol}^{-1}$	$H_{\rm m,123}^{\rm E}/{ m J}~{ m mol}^{-1}$	$x_1$	$x_2$	$H_{\mathrm{m,\phi}}^{\mathrm{E}}/\mathrm{J} \mathrm{mol}^{-1}$	$H_{\rm m,123}^{\rm E}/{ m J}~{ m mol}^{-1}$
$x_1'=0.2558, H_{m12}^{E}=213 \text{ J mol}^{-1}$							
0.2314	0.6732	454	647	0.0899	0.2615	1089	1164
0.2108	0.6133	715	891	0.0765	0.2226	1011	1075
0.1745	0.5077	1035	1181	0.0598	0.1740	873	923
0.1497	0.4355	1146	1271	0.0477	0.1388	746	786
0.1373	0.3994	1167	1282	0.0332	0.0967	571	598
0.1231	0.3583	1164	1267	0.0233	0.0679	424	444
0.1075	0.3127	1160	1250	0.0140	0.0408	270	282
$x_1'=0.5038, H_{m,12}^{E}=319 \text{ J mol}^{-1}$							
0.4554	0.4485	314	602	0.2145	0.2113	811	947
0.4215	0.4151	474	740	0.1909	0.1880	779	900
0.3881	0.3822	601	846	0.1517	0.1494	705	801
0.3543	0.3489	698	922	0.1191	0.1173	615	691
0.3138	0.3090	774	973	0.0777	0.0765	453	503
0.2863	0.2819	803	984	0.0550	0.0542	344	379
0.2617	0.2577	833	998	0.0311	0.0307	210	229
$x_1'=0.7531, H_{m,12}^{E}=277 \text{ J mol}^{-1}$							
0.6836	0.2241	161	412	0.2755	0.0903	420	521
0.6457	0.2117	232	470	0.2912	0.0955	424	531
0.6111	0.2003	291	516	0.2141	0.0702	365	443
0.5336	0.1749	377	573	0.1604	0.0526	303	362
0.4934	0.1617	410	591	0.1170	0.0383	239	282
0.4616	0.1513	427	597	0.0902	0.0296	192	225
0.3914	0.1283	442	586	0.0518	0.0170	121	140
0.3504	0.1149	451	580				

<sup>a</sup>Three experimental series of measurements were carried out for the ternary compositions resulting from adding diethyl carbonate to a binary mixture composed of  $\{x_{i}^{t}p$ -xylene+ $x_{2}^{t}$  decane}, where  $x_{2}^{t}=1-x_{1}^{t}$ .

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$B_0$	$B_1$	$B_2$	<i>B</i> <sub>3</sub>	$B_4$	S		
$x_1p$ -xylene+ $x_2$ decane+ $x_3$ diethyl carbonate							
4060	0	-6931	0	8710	7		



Fig. 3 Representation for { $x_1p$ -xylene+ $x_2$ decane+(1- $x_1$ - $x_2$ ) diethyl carbonate} at 298.15 K of: a – curves of constant ternary excess molar enthalpy,  $H_{m,123}^{E}/J$  mol<sup>-1</sup>, b – curves of constant ternary contribution,  $x_1x_2(1-x_1-x_2)\Delta_{123}$ , to the excess molar enthalpy  $H_{m,123}^{E}/J$  mol<sup>-1</sup>, calculated with Eq. (6)

Excess molar enthalpy for the ternary system is positive over the whole range of composition, showing maximum values at  $x_1=0$ ,  $x_2=0.4920$ ,  $x_3=0.5080$ ,  $H_{m,123}^{E}=1524 \text{ J mol}^{-1}$ .

The ternary contribution is also positive, and the representation is symmetric. That means that, as can be seen in Fig. 3b, the position of the maximum coincides with the centre of the Gibbs triangle. There is a maximum value at  $x_1=0.3571$ ,  $x_2=0.2857$ ,  $x_3=0.3572$ ,  $H_{m,123}^{E}=102$  J mol<sup>-1</sup>. The value of maximum ternary contribution is about 7% of the value of the ternary enthalpy itself. Thus, excess molar enthalpy in the

ternary mixture can be probably ascribed to the effects that occur in the binary ones. Maximum value of the excess molar enthalpy is due to the contribution of the binary system {xdecane+(1-x)diethyl carbonate}, where the predominant effect is the destruction of the dipolar order of the diethyl carbonate during mixing process.

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## References

- L. Mosteiro, E. Mascato, B. E. de Cominges, T. P. Iglesias and J. L. Legido, J. Chem. Thermodyn., 33 (2001) 787.
- 2 L. Mosteiro, E. Mascato, D. González-Salgado B. E. de Cominges and M. M. Piñeiro, J. Therm. Anal. Cal., 70 (2002) 255.
- 3 I. García, J. C Cobos, J. A. González and C. Casanova, Int. DATA Ser. Sel. Data Mixtures, Ser. A, 3 (1987) 164.
- 4 P.-J. Lien, H.-M. Lin, M.-J. Lee and P. Venkatesu, Fluid Phase Equilib., 206 (2003) 105.
- 5 M. Domínguez-Pérez, J. Jiménez de Llano, L. Segade, C. Franjo and O. Cabeza, J. Therm. Anal. Cal., 80 (2005) 289.
- 6 CRC Handbook of Chemistry and Physics. CRC Press, 84<sup>th</sup> Edition, 2003–2004.
- 7 IUPAC, Pure Appl. Chem., 58 (1986) 1677.
- 8 M. I. Paz Andrade, Les Dévelopements Récents de la Microcalorimétrie et de la Thermogenèse, 1<sup>st</sup> Ed.; CRNS, Paris 1967.
- 9 M. I. Paz Andrade, S. Castromil and M. C. Baluja, J. Chem. Thermodyn., 2 (1970) 775.
- 10 O. Redlich and A. T. Kister, Ind. Eng. Chem., 40 (1948) 345.
- 11 D. W. Marquardt, J. Soc. Ind. Appl. Math., 2 (1963) 431.
- 12 P. Bevington, Data Reduction and Error Analysis for the Physical Sciences, McGraw-Hill, New York 1991.
- 13 I. Nagata and K. Tamura, J. Chem. Thermodyn., 22 (1990) 279.

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